
LONG-RUN IMPLIED MARKET FUNDAMENTALS: AN EXPLORATION

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The paper studies the volatility and correlation pattern of the fundamental valuation parameters (growth rate and its determinants, discount rate) calculated from widely used valuation ratios using the Gordon formula, and compares the findings to well-known insights from the asset pricing literature. Our results reveal a substantially different picture of the volatility and cyclical nature of the implied valuation parameters compared to estimates from econometric models using historical returns. We argue, in the spirit of Campbell (2008), that implied Gordon parameters can be interpreted as empirical proxies for conditional steady-state market fundamentals, which is supported by our findings. The insights of this paper are therefore particularly challenging for investors with a long-term investment horizon who base their decisions on fundamental valuation factors.



"Steady-state valuation models are useful predictors of stock returns, given the persistence in valuation ratios." Campbell (2008)

In times of low—and in Europe, negative—interest rates and high stock market valuations, the fundamental analysis of equities is becoming increasingly important. In a previous paper published in this *Journal*, Zimmermann (2018) suggested to estimate the three fundamental,

unknown parameters of the Gordon equity valuation model from three fundamental valuation ratios widely used in the investment practice. While this approach is simple and obvious, it seems to be novel and provides interesting insights. For example, in spite of the sensitivity of Gordon prices with respect to the input variables, the implied parameter estimates exhibit reasonable values and are surprisingly stable.

In this paper, we take this analysis a step further and study the volatility and correlation pattern of the implied Gordon-parameters (respectively, their first differences) and relate them to some well-known results from the asset pricing literature: the use of dividend–price ratios as proxies

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for expected returns, the cyclicity of risk premiums, and the predictions of the long-run risk (LRR) models.

Our empirical findings are in sharp contrast to the asset pricing literature: The implied Gordon parameters predict a substantially larger volatility of growth rates than most predictive models, and the growth rate is positively and occasionally extremely highly correlated with the discount rate. These observations have important implications for the valuation of equities: For example, the positive association between changes in growth and discount rates suggests a completely different interpretation of the cyclicity of risk premiums compared to, for example, conditional asset pricing models estimated with typical state variables (“business conditions”). We hypothesize that our risk premiums are related to long-run growth risk. However, the dynamic properties of our implied parameters even contrast the findings of the long-run risk models. Apparently, information extracted from valuation ratios, using simple valuation models, differs considerably from the estimates relying on econometric models using historical returns.

While our procedure may be justified by pragmatic or practical reasons, it however seems to suffer from a methodological problem: the derivation of time-varying parameters from a model which assumes that they are constant. We address this problem by building on an interesting insight from Campbell (2008) and interpret the implied parameters as proxies for steady-state market fundamentals. We observe that all parameters (in levels) are highly persistent which strongly supports our interpretation.

The paper is structured as follows: Section 1 starts with a numerical example illustrating the calibration of the Gordon formula with observed valuation ratios. Section 2 documents the statistical properties of the Gordon-implied parameters,

and Section 3 highlights the implications for equity valuation, notably the size and cyclicity of discount rates and risk premiums. Section 4 discusses the adequacy and justification of the Gordon model for extracting time-varying parameters and their interpretation as steady-state valuation proxies. In Sections 5 and 6, the major findings are briefly reviewed and some implications are addressed.

1 A Numerical Example to Start

We estimate the three unobservable parameters from the Gordon constant growth valuation formula from three widely used valuation ratios applied to stock market indices (D/P , P/E , and P/B). The Gordon model assumes that earnings and dividends grow by a constant rate $w = rb$, where b is the fraction of earnings reinvested at the end of each year, and r is the profitability of the reinvested earnings (i.e. the return on equity ROE). Therefore, $1 - b$ is the dividend payout ratio.

The stock price is then given by the present value of the perpetual stream of constantly growing dividends, using a constant discount rate k strictly larger than the growth rate w :

$$P = \frac{D}{k - w} = \frac{E(1 - b)}{k - rb} \quad (1)$$

where D and E are the dividend and earnings levels, respectively, at the end of the current period, which can be observed (or can at least be predicted more or less accurately) using the valuation ratios. In contrast, the long-run parameters k , r and b are unknown and must be estimated.

From the Gordon formula, the implied D/P - and P/E -ratios can be easily derived, namely¹

$$\frac{D}{P} = k - rb = k - w, \quad \frac{P}{E} = \frac{1 - b}{k - rb} \quad (2)$$

The book-to-price ratio requires an additional assumption: profitability is typically related to the

book value by $r = E/B$, such that the B/P -ratio implied by the Gordon formula is

$$\frac{P}{B} = \frac{r - rb}{k - rb} \quad (3)$$

As shown in Zimmermann (2018), the three unknowns k , r and b in the Gordon formula (and w , which is however redundant) can be easily related to these ratios. The discount rate is

given by

$$k = \frac{D}{P} + w = \frac{D}{P} + \frac{P}{B} \cdot \left(\frac{1}{\frac{P}{E}} - \frac{D}{P} \right) \quad (4)$$

which also defines the implied growth rate. The implied profitability is

$$r = \frac{E}{B} = \frac{P/B}{P/E} \quad (5)$$

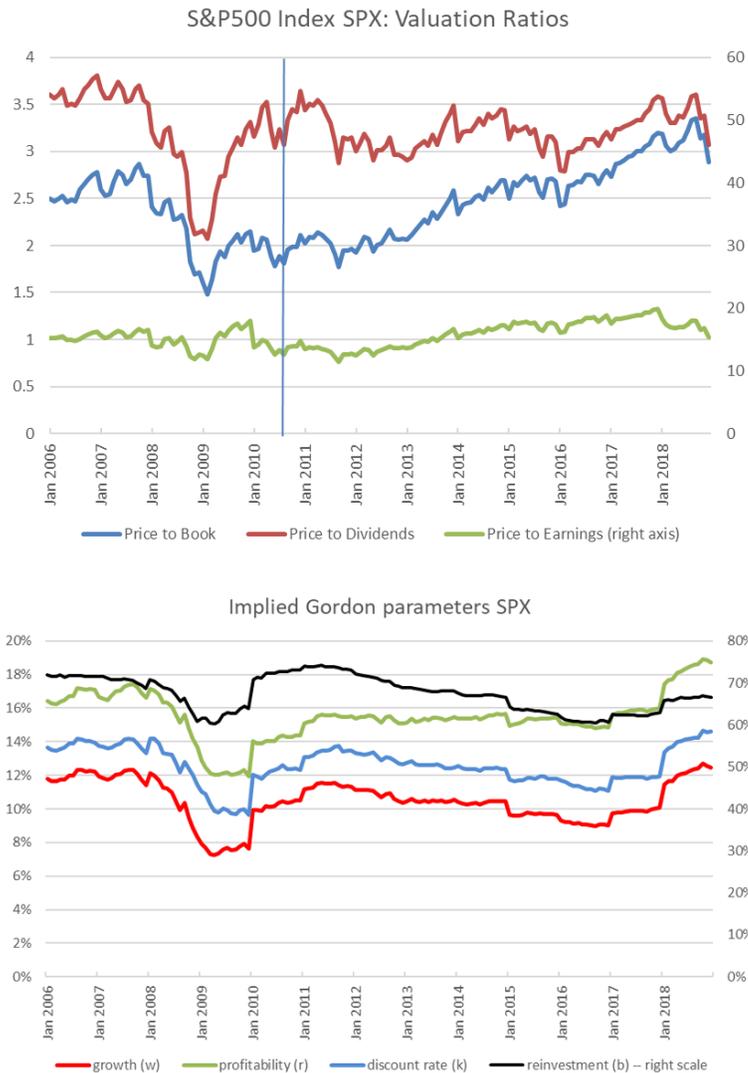


Figure 1 Valuation Ratios and Implied Parameters from the Gordon Formula.

The reinvestment rate (b), profitability (r), growth (w) and discount rate (k) are extracted from three valuation ratios (price–earnings, price–dividend, price–book) using the Gordon model. S&P500 multiples are downloaded from Bloomberg. Monthly data are used from January 2006 to December 2018.

while the implied reinvestment rate can be recovered from $b = w/r$. For example, the year-end values as of December 2018, after a temporary decline of the stock markets, the ratios for the S&P500 index as released by Bloomberg (see the Appendix for details) are

$$\frac{D}{P} = 0.0217, \quad \frac{P}{E} = 15.4, \quad \frac{P}{B} = 2.9$$

which leads to the following parameters:

$$\begin{aligned} r &= 0.187, & b &= 0.665 \\ w &= 0.124, & k &= 0.146 \end{aligned}$$

The implied payout ratio is 33.5%.

Figures 1 and 2 display the evolution of the three valuation ratios for the S&P500 and their implied parameters. For consistency with the other two ratios, the inverse of the D/P is displayed. At the first glance, the implied growth rate and discount rate are highly correlated, which mirrors the low variability of the D/P -ratio. This observation is further analyzed in the next section.

The *joint* interpretation of the valuation ratios with respect to the underlying fundamental parameters is a key feature of that approach and was discussed in Zimmermann (2018). While it is common practice to base fundamental views on individual ratios (e.g. an increase in the P/E -ratio to indicate accelerated growth), the approach here shows different results. For example, take the year-end valuation ratios one year earlier in the previous example, at the end of December 2017:

$$\frac{D}{P} = 0.0186, \quad \frac{P}{E} = 19.9, \quad \frac{P}{B} = 3.2$$

The Gordon formula implies

$$\begin{aligned} r &= 0.160, & b &= 0.629 \\ w &= 0.100, & k &= 0.119 \end{aligned}$$

The P/E -ratio declined from 19.9 to 15.4, but the implied growth rate experienced an *increase* from 10% to 12.4%! Therefore, neglecting the

information from the other two ratios can lead to misinterpretation. The P/E -ratio in isolation does not reveal that the anticipated profitability of US firms increased from 16% to 18.7% during that year, and neglecting the D/P -ratio makes it impossible to infer the implied growth and discount rates, and their change.

2 Statistical Properties of Gordon-Implied Parameters

The descriptive statistics of the first differences of the implied parameters are displayed in Tables 1 and 2.² The same four stock markets are analyzed as in the earlier study (US, Germany, Switzerland, and Europe). The overall observation is that the implied parameters behave quite smoothly over time, which is not an obvious result given the strong sensitivity of the Gordon-implied prices and price ratios with respect to the underlying parameters, in particular if the denominator of the formula, the dividend–price ratio, is small.

A key observation is that the dividend–price ratio is much more stable than the underlying Gordon parameters, i.e. the discount rate and the growth rate, as summarized in Table 3. For the US market, the D/P -ratio exhibits a volatility of 0.098% or approximately 0.1%, while the implied growth rate has a volatility of 0.31% which is in the same order of magnitude as the volatility of the discount rate (0.32%). This observation is most pronounced for the US and Switzerland, and less for the German and European markets. For the first two markets, the volatilities of the implied parameters are sizeable compared to the relative stability of the D/P -ratio. The explanation can be immediately seen from variance decomposition³

$$\begin{aligned} &\text{Var} \left(\Delta \frac{D}{P} \right) \\ &= \text{Var}(\Delta k) + \text{Var}(\Delta w) - 2\text{Cov}(\Delta k, \Delta w) \\ &= 0.09418 + 0.09959 - 0.18412 \\ &= 0.009653 \end{aligned} \tag{6}$$

Table 1 Descriptive Statistics of Implied Gordon Parameters, First Differences.

		Mean	Volatility	AC(1)	AC(2)	AC(3)	AC(6)	AC(12)	$p(LB, 12)$
Reinvestment Δb	SMI	-0.0016	0.0219	-0.13	-0.07	-0.08	0.04	0.30	0.000
	S&P500	-0.0003	0.0082	0.08	0.07	0.24	0.06	0.21	0.004
	DAX	-0.0004	0.0104	0.11	0.10	0.30	0.11	0.09	0.002
	EUROSTOXX50	-0.0006	0.0077	0.11	0.07	0.09	-0.09	-0.04	0.351
Profitability Δr	SMI	-0.0003	0.0072	-0.10	-0.02	-0.09	0.23	0.26	0.001
	S&P500	0.0001	0.0030	0.09	0.13	0.20	0.11	0.09	0.094
	DAX	-0.0001	0.0030	0.17	0.10	0.31	0.20	-0.06	0.000
	EUROSTOXX50	-0.0003	0.0025	0.30	0.25	0.29	0.02	-0.03	0.000
Growth Δw	SMI	-0.0004	0.0067	-0.11	-0.02	-0.09	0.17	0.32	0.000
	S&P500	0.0000	0.0031	0.07	0.10	0.22	0.09	0.14	0.057
	DAX	-0.0001	0.0026	0.19	0.10	0.29	0.19	0.01	0.000
	EUROSTOXX50	-0.0002	0.0020	0.21	0.18	0.21	-0.02	-0.03	0.011
Discount rate Δk	SMI	-0.0003	0.0072	-0.12	-0.05	-0.12	0.11	0.39	0.000
	S&P500	0.0001	0.0032	0.01	0.00	0.17	-0.01	0.16	0.158
	DAX	0.0000	0.0034	0.08	-0.11	0.22	-0.03	0.12	0.062
	EUROSTOXX50	-0.0002	0.0032	0.08	-0.06	0.12	-0.21	0.06	0.019

Notes: The displayed statistics are means, volatilities, and autocorrelations (AC) at lags 1, 2, 3, 6, and 12 of first differences of reinvestment rate (b), profitability (r), growth (w) and discount rate (k) which are extracted from three valuation ratios (price–earnings, price–dividend, price–book) using the Gordon model. SMI refers to the Swiss stock market, S&P500 to the US stock market, DAX to the German stock market and EUROSTOXX50 to the major stocks of the Euro area. Monthly data are used from January 2006 to December 2018. Bold figures indicate 95% significance. $p(LB)$ is the p value of the Ljung–Box test for 12 lags, bold values: AC = 0 rejected.

Table 2 Correlations between Implied Gordon Parameters, First Differences.

	Δb	Δr	Δw	Δk	Δb	Δr	Δw	Δk
	SMI				S&P500			
Δb	1.000				1.000			
Δr	0.865	1.000			0.836	1.000		
Δw	0.940	0.976	1.000		0.928	0.979	1.000	
Δk	0.923	0.963	0.981	1.000	0.881	0.932	0.951	1.000
	DAX				EUROSTOXX50			
Δb	1.000				1.000			
Δr	0.778	1.000			0.681	1.000		
Δw	0.907	0.962	1.000		0.868	0.948	1.000	
Δk	0.749	0.774	0.790	1.000	0.499	0.643	0.625	1.000

Notes: The reinvestment rate (b), profitability (r), growth (w) and discount rate (k) are extracted from three valuation ratios (price–earnings, price–dividend, price–book) using the Gordon model. SMI refers to the Swiss stock market, S&P500 to the US stock market, DAX to the German stock market and EUROSTOXX50 to the major stocks of the Euro area. Monthly data are used from January 2006 to December 2018.

Table 3 Volatility of the Dividend-price Ratio and its Constituents (k , w).

	Volatility			Correlation
	$\Delta D/P$	Δk	Δw	$(\Delta k, \Delta w)$
SMI	0.147%	0.723%	0.666%	0.981
S&P500	0.098%	0.316%	0.307%	0.951
DAX	0.206%	0.336%	0.261%	0.790
EUROSTOXX50	0.249%	0.318%	0.199%	0.625

Notes: The reinvestment rate (b), profitability (r), growth (w) and discount rate (k) are extracted from three valuation ratios (price–earnings, price–dividend, price–book) using the Gordon model. SMI refers to the Swiss stock market, S&P500 to the US stock market, DAX to the German stock market and EUROSTOXX50 to the major stocks of the Euro area. Monthly data are used from January 2006 to December 2018.

which reveals the role of the positive covariance (the correlation is 0.95) between the two parameters. For the Swiss stock market, the correlation is even close to 1, while it is close to 0.8 for the German market and slightly above 0.6 for the Eurostoxx50.

Two observations are important from these results: First, there is a substantial variation in implied growth rates, and second, the growth rate is positively and occasionally extremely highly correlated with the discount rate. This has important implications with respect to the valuation of equities and contrasts similar findings in the empirical literature:

3 Implications for Equity Valuation

3.1 Changes of k as a proxy for revisions in expected returns?

The variability of w is often ignored—or played down—in the empirical asset pricing literature. In an important paper about the equity premium in the second half of the 20th century, Fama and French (2002) concluded that the high average returns over the observed period are mainly driven by declining expected returns, extracted from the D/P -ratio, so that the average returns

are largely interpreted as *unexpected*. Of course, the variability of the expected growth rate invalidates the interpretation of variations of D/P -ratios as a direct proxy of revisions in expected returns.

The implications can be illustrated using two examples displayed in Table 4. The first example highlights the valuation of the Swiss stock market (proxied by the SMI) at the end of 2006 and 2008, i.e. the period covering the outbreak of the financial crisis with substantial drop of stock prices. The D/P -ratio sharply increased over the two years from 2% to 3.1% suggesting that down-revisions of stock prices were stronger than declines in dividends. This increase was, however, not paralleled by an upward revision of the expected return (discount rate), quite the contrary can be observed: it declined from 14.6% to 7.1%. How can this be reconciled with a substantial drop in stock market prices? Apparently, the expected growth rate declined even more, namely from 12.6% to 4%.⁴

The second example relates to the valuation of the German stock market (proxied by the DAX) at the end of 2010 and 2017, a period when the index more than doubled. The D/P -ratio declined from 3.7% to 2.8%, while the expected return remained

Table 4 Are Changes in D/P a Good Proxy for Changes in Discount rates?

		Valuation Ratios			Implied Gordon Parameters			
		P/E	P/B	D/P	$1 - b$	r	w	k
SMI	Dec 2006	16.8	3.2	2.0%	33.6%	19.0%	12.6%	14.6%
	Dec 2008	19.3	1.9	3.1%	59.8%	9.8%	4.0%	7.1%
DAX	Jan 2010	12.1	1.4	3.7%	45.0%	11.3%	6.2%	9.9%
	Dez 2017	14.6	1.8	2.8%	41.5%	12.1%	7.1%	9.9%

Notes: The reinvestment rate (b), profitability (r), growth (w) and discount rate (k) are extracted from three valuation ratios (price–earnings, price–dividend, price–book) using the Gordon model. SMI refers to the Swiss stock market, S&P500 to the US stock market, DAX to the German stock market and EUROSTOXX50 to the major stocks of the Euro area. Monthly data are used from January 2006 to December 2018.

constant (9.9%). The rise of the stock market was exclusively caused by a moderate increase in growth expectations from 6.2% to 7.1%. Again, a shorthand interpretation based on changes in the D/P -ratio is misleading.

The examples highlight how important it is to incorporate the interaction of *several* valuation multiples into a model-based approach to reach meaningful conclusions about the fundamental forces driving equity values.

3.2 Cyclicalities of risk premiums

The preceding analysis has direct implications for the interpretation of risk premiums over stock market cycles. The conventional message from the Conditional Asset Pricing Model as pioneered by Ferson and Harvey (1991) and others is that risk premiums are high in bad economic states and low in good states. State variables such as interest rate spreads (long minus short, credit, TED), valuation multiples or macroeconomic data are used for modeling the time-varying state of the economy.

The positive correlation coefficients between the changes in discount and growth rates (Δk , Δw) as shown in Table 2 (and 3) already indicate a different pattern in our data. On average, good news, i.e. more optimistic growth rates,

occur together with positive revisions in expected returns. Table 5 reveals that this pattern also translates to the risk premiums as exemplified by the 1994–2004 decade covering a remarkable stock market boom and the subsequent dotcom-crash. The expected risk premium is calculated as the discount rate minus the long-run T-Bond yield.⁵ The figures reveal an increasing—not decreasing—equity premium in the years before 2000 which is paralleled by an increase of the expected growth rate. With regard to Fama and French (2002), at last some of the sizeable stock market returns of the roaring nineties were expected, not unexpected! This misattribution is a consequence of assuming constant (or “stationary”) growth expectations.

The years of the burst of the dotcom bubble reveal a mixed picture. In 2001, the risk premium sharply declined, along with the growth expectation, but the subsequent reversals are difficult to reconcile with a simple theory. But still, we observe a strong positive association between expected risk premiums and growth expectations, which completely contradicts—at least at first sight—the standard explanation for the fluctuation of risk premiums.

However, the results are not necessarily inconsistent because the expected returns, and risk

Table 5 Implied Gordon Parameters and Expected Risk Premiums S&P500, 1994–2004.

Year	Index S&P500	Valuation Ratios			Implied Gordon Parameters				Exp Risk Premium	
		D/P	P/E	P/B	k	w	r	$1 - b$	int	rp
1994	459	1.71%	16	1.7	9.2%	7.5%	10.3%	27.4%	7.8%	1.4%
1995	616	1.52%	18.9	2.1	9.4%	7.8%	11.0%	28.7%	5.7%	3.7%
1996	741	1.49%	19.2	2.3	9.9%	8.4%	11.8%	28.6%	6.3%	3.6%
1997	970	1.10%	23.7	3.3	11.3%	10.2%	13.8%	26.1%	5.8%	5.5%
1998	1229	1.44%	22.7	3.5	11.8%	10.4%	15.4%	32.7%	4.7%	7.2%
1999	1469	1.28%	20.5	3.3	13.0%	11.8%	16.0%	26.2%	6.3%	6.8%
2000	1320	1.38%	19.5	3.3	13.8%	12.4%	17.0%	26.9%	5.2%	8.6%
2001	1148	1.92%	19.4	2.6	10.3%	8.4%	13.4%	37.2%	5.1%	5.2%
2002	880	1.48%	16.3	2.5	13.0%	11.5%	15.2%	24.1%	4.0%	8.9%
2003	1112	1.53%	21	2.4	9.4%	7.9%	11.6%	32.1%	4.3%	5.1%
2004	1212	1.66%	14.4	2.4	13.0%	11.4%	15.3%	25.6%	4.2%	8.8%

Notes: The fundamental ratios are from Datastream and are year-end values of the S&P500 index. The reinvestment rate (b), profitability (r), growth (w) and discount rate (k) are extracted from three valuation ratios (price–earnings, price–dividend, price–book) using the Gordon model. “int” denotes the yield on US government bonds with a maturity of 20 years and is used as proxy for the long-run risk-free rate; “rp” is the expected risk premium.

premiums, are related to different time horizons. The forecast horizon of conditional asset pricing models is typically a month, or one year at most. The implied Gordon parameters, however, are related to an infinite time horizon. Therefore, the information extracted from the Gordon model need not to be consistent with the short-run expectations modeled by standard asset pricing models with conditioning information. Rather, the expected returns—respectively risk premiums—identified in the Gordon setting are most likely related to *long-run growth* risk. The intuition may be as follows: The sensitivity of the Gordon equity price with respect to a small change in the underlying growth rate is

$$\frac{\partial P}{\partial w} = \frac{D}{(k - w)^2} = P \frac{1}{k - w}$$

and the relative sensitivity, i.e. growth risk of equity, is

$$\frac{\partial P/P}{\partial w} = \frac{1}{k - w} \quad (7)$$

Notice that the denominator is the dividend–price ratio. Typically, the D/P -ratio decreases during a boom and increases in economic downturns. Therefore, if business conditions improve (worsen), the denominator gets smaller (larger) and growth risk increases (decreases). This explains a pro-cyclical behavior of growth risk, but not yet a pro-cyclical risk premium. This link is addressed later (Section 3.4).

3.3 Statistical long-run risk (LRR) models: A comparison

Following the excess volatility dispute originated by Shiller (1981), a large body of research has analyzed the long-run effects of small, but persistent fundamental shocks in the modeling of security prices and cross-sectional returns; the shorthand “LRR-models” is used subsequently.⁶ A particularly interesting strand of research demonstrates that excess volatility of prices with respect to fundamental factors (dividends, earnings) can be tested using valuation *ratios*, and

the variability of these ratios must be related to the predictability of the underlying fundamentals in a rational market. Following the decomposition developed by Campbell and Shiller (1988), a large number of papers have empirically analyzed the predictive power of valuation ratios, in particular the D/P -ratio, with respect to long-run (infinite horizon) discount rates and growth rates. The tests have been conducted in various econometric settings (simple predictive regressions, VAR-systems, advanced predictive systems) and generated rather contradictory results. A particularly interesting test is presented by Cochrane (2008) who finds that dividend growth (w) is not predictable from D/P -ratios, which he interprets—armed with Sherlock Holmes’ line of reasoning—as indirect but strong evidence for predictability of discount rates (k). While not directly comparable with our results, it is a surprising finding in the light of the strong volatility of the implied grow rates shown in Table 1. However, recent studies such as Chen *et al.* (2012) demonstrate that dividend smoothing masks a substantial part of the predictability of w , should it exist.

A related test approach is proposed by Campbell (1991) where predictability of valuation ratios is tested by a variance decomposition of asset returns. This decomposition is derived from the residuals of a vector autoregressive (VAR) model which includes, apart from asset returns and dividend growth rates, state variables for modeling conditional expectations over time such as valuation ratios or macroeconomic indicators. A major output of this model are so called “news”, i.e. updates of conditional expectations about an infinite sequence of future discount rates (DR) and growth rates (of cash flows, CF).⁷ This approach seems, at first sight, closely related to the approach of this paper because our implied parameters can be interpreted as periodic updates of long-run expectations about the underlying

fundamentals. We are therefore tempted to associate Campbell’s DR-news with updates for k and CF-news with updates for w .

However, the empirical findings differ substantially, in particular with respect to the correlation coefficients between the news. This is a key magnitude for analyzing D/P - and return-volatilities. In his original study (Table 2), Campbell finds strongly negative correlations over the overall time period (-0.53) and two subperiods (-0.66 , -0.16). The explanation is straightforward and in the spirit of conditional asset pricing models: Good news about future growth imply lower expected returns. However, this contradicts our findings from Sections 2 and 3.2 where we report (strong) positive correlations between Δw and Δk . Such negative values would be entirely inconsistent with the low volatility of the D/P -ratio observed in our data, as can be seen from our numerical example in Equation (6).

Campbell uses real data in his original paper from 1926 to 1988, while our analysis is based on nominal magnitudes for a more recent time period. We therefore take the nominal news-data (which are available online) of Campbell and Vuolteenaho (2004) and provide a variance decomposition in the Campbell (1991)-style. The results are displayed in Table 6 and reveal correlation coefficients between -0.057 and 0.140 , depending on the time period. The coefficients are less negative than in the Campbell study, but still substantially smaller than those reported for the implied Gordon parameters in Table 2 (between Δw and Δk).⁸

The correlation between the updates of fundamental expectations—be it “news” or implied Gordon parameters—is an important determinant of the variability of the D/P -ratio, but also determines the volatility of stock returns. The simple reason is that the D/P -ratio shows up in the denominator of the Gordon price-formula ($k - w$), so that even

Table 6 A Detailed Analysis of the Campbell–Vuolteenaho CF- and DR-news.

	Variance Decomposition					Autocorrelation							
	N	var CF_N	var DR_N	-2cov	corr	CF_N	DR_N	AC(1)	AC(2)	AC(3)	AC(6)	AC(12)	<i>p(LB)</i>
Full time period, 12:1928–12:2001	876	0.064	0.267	-0.030	0.114	CF_N -0.289	DR_N -0.054	0.061	-0.033	-0.012	0.020	0.049	0.000
Subperiod 1, 12:1928–12:1952	288	0.110	0.405	0.024	-0.057	CF_N -0.294	DR_N -0.006	0.054	-0.039	-0.004	0.078	0.064	0.000
Subperiod 2, 01:1953–12:1977	300	0.035	0.166	-0.043	0.140	CF_N -0.282	DR_N -0.133	0.079	-0.021	0.103	-0.084	-0.082	0.000
Subperiod 3, 01:1978–12:2001	288	0.047	0.236	-0.068	0.082	CF_N -0.293	DR_N -0.090	0.057	-0.033	-0.129	-0.044	0.112	0.000

Notes: The monthly “news” data are downloaded from the AEA (American Economic Association) website and cover the time period 1928 to 2001. CF_N denote cash-flow news, DR_N denote discount rate news. Variances and covariances are multiplied by 100. *p(LB)* is the *p* value of the Ljung–Box test for 12 lags, bold values: AC = 0 rejected.

small variations are associated with large price adjustments, i.e. volatile returns. A strong negative correlation between CF- und DR-news would inflate the volatility of *D/P*-ratios and therefore increase the variability of stock returns. In contrast, our correlations which are higher than 0.9 for the US and Swiss stock market exert a dampening influence on the stock return volatilities. Thus, stock returns may still be very volatile relative to the underlying economic fundamentals and their expectations, but the correlation pattern seems to have a stabilizing effect. This insight is all the more interesting as the Gordon model assumes an infinitely long-time horizon.

Finally, a puzzling observation is worth emphasizing. When interpreting DR- and CF-news, the permanent and transitory nature of the two components is often considered as a key distinguishing characteristic. For example, Campbell and Vuolteenaho (2004) claim that “these return components can also be interpreted approximately as permanent and transitory shocks to wealth. Returns generated by cash flow news are never reversed subsequently, whereas returns generated by discount rate news are offset by lower returns in the future.” (p. 1252). The autocorrelation

coefficients at the first lag in Table 6 (which are not shown in the cited paper) are indeed sizeable and in more cases significant for the CF-news in contrast to the DR-news, but with a negative sign! This observation can hardly be reconciled with what is typically regarded as a permanent shock. Rather a negative sign indicates a short-run overreaction to long-run CF-related information. Interestingly, similar coefficients are not present in our implied parameters in Table 1. While negative values are estimated for the SMI (about -0.10), the values for the other markets are close to zero (for Δk) or slightly positive (for Δw , 0.07 to 0.12), but not statistically significant. Therefore, while far from permanent, the pattern of the shocks corresponds more closely to the hypothesized effects in Campbell and Vuolteenaho’s quote.

Overall, the statistical properties of LRR-innovations (“news”) in expected returns and discount rates are completely different from those implied by the Gordon model. Although the LRR-models seem to be closely related to the Gordon-approach, it is important to notice that they rely on simple return-identities complemented by an expectation formation mechanism,

and cannot be regarded as valuation models. They are based on estimates from historical data, dividend growth, asset returns, and state variables (as proxies for the conditioning information set of expectations)—which is distinct from our approach which rests entirely on observed valuation ratios *and* an explicit valuation model. The Gordon formula may be oversimplified, but it allows to calibrate the parameters without relying on historical data and estimation issues. As Campbell (2008) puts it, “the approach is analogous to the familiar procedure of forecasting the return on a bond, using its yield rather than its historical average return” (p. 8). This is exactly the intuition underlying our approach.

3.4 A growth-related risk premium?

The previous remarks suggest a comparison of our results to *valuation* models which explicitly take into account long-run risk factors, specifically growth risk (CF-news). The task is to reconcile an increase in the expected growth rate (w) with a higher (growth) risk premium and hence a positive shift in expected returns (k). The Bansal and Yaron (2004) model offers such a framework. Conditional expected returns are related to the conditional covariance of returns with innovations in long-run expected growth rates (CF-news).⁹ For market indices, as analyzed here, a positive covariance can be assumed. As suggested by Equation (7), the temporal behavior of the D/P -ratio implies that the variance of returns is positively related to upward revisions in the expected growth rate, i.e. to good economic states. *Ceteris paribus*, this implies that the covariance between market returns and CF-news increases if the state of the economy improves.

An increase in the covariance implies a positive effect on expected returns only if the market price of growth risk is positive. In the Bansal–Yaron model this is only the case if a specific condition

is satisfied, namely¹⁰

$$\gamma - \frac{1}{\psi} > 0$$

where γ is the standard relative risk aversion coefficient and ψ denotes the elasticity of intertemporal substitution (EIS) of income. The condition stipulates that the curvature of the utility function with respect to uncertain income must be stronger than with respect to the safe intertemporal stream of income, and is tantamount to a preference for early—as opposed to late—resolution of uncertainty. This condition plays a major role in LRR-pricing models and is highly controversial because it requires, for low aggregate levels of risk aversion, pretty high levels of EIS which seems to contradict many empirical estimates.¹¹

However, the condition fully supports our observation of a positive correlation between Δw and Δk , motivated by a higher growth risk premium in times of elevated expected growth. Of course, the Bansal–Yaron framework is just one of several possible ways to analyze this relationship, and the remarks in this Section are no more than an attempt to offer a possible explanation of our empirical finding.

4 Gordon Model and Steady-State Dynamics

Is there a way to reconcile the Gordon formula with the LRR-models? Even more fundamentally: Is the Gordon model an adequate framework at all for extracting time-varying parameters? After all, the model assumes constant parameters, and unlike the LRR-models, no uncertainty enters the formula. When using the Gordon formula, it is just common practice to specify k and w as long-run expected returns and dividend growth, but this is done on an ad-hoc basis without modeling the underlying uncertainty—and the same is done in this paper by extracting the

“implied” parameters and by interpreting them as long-term expectations. Is there a theoretical basis for such an interpretation? There are indeed theoretical papers addressing the impact of uncertainty in the dividend growth process on the *level* of stock prices—e.g. Ziegler (2001) in an attempt for explaining the dot-com bubble—but they do not offer a simple justification for such an interpretation.

4.1 Geometric versus arithmetic interpretation of the Gordon parameters

The paper by Campbell (2008) seems to provide the missing link. The starting point of the model is the empirical observation that the (logarithmic) dividend–price process is typically very close to a Random Walk, i.e. shocks to *D/P*-levels are expected to be largely permanent. The autocorrelations in Table 7 support this observation, although the coefficients at the first lag are well below unity.¹² However, they are declining slowly, and the ADF-test cannot reject a unit root on a 90% confidence level. Therefore, *D/P*-processes exhibit a high degree of persistence.

Two assumptions are key in Campbell’s model: First, the log *D/P*-process follows a Random

Walk; and second, the two sources of uncertainty, log *D/P* growth and log dividend growth, are conditionally normally distributed.¹³ The non-stationarity of the *D/P*-ratio invalidates the usual log-linear approximations underlying the Campbell-Shiller or Campbell-decompositions, but instead, a strikingly simple approximation can be derived which relates the conditional expectations of logarithmic returns (r_{t+1}) and logarithmic dividend growth (Δd_{t+1}), namely

$$e^{E_t(r_{t+1})} \approx \frac{D_{t+1}}{P_t} + e^{E_t(\Delta d_{t+1})} \quad (8)$$

The approximation (8) is a restatement of Campbell’s eq. (21):¹⁴ The l.h.s. is the geometric analog to (one plus) the expected return or discount rate, the second expression of the r.h.s. the geometric analog to (one plus) the expected dividend growth rate.

The two geometric expressions can be expanded to an infinite future time horizon by applying the Law of Iterated Expectations and recognizing that the statistical relationship between the expectation of a geometric average, \bar{X}_g , and the expectation of the natural logarithm, $x = \ln(1 + X)$, is given by

$$\lim_{n \rightarrow \infty} E_t(1 + \bar{X}_g) = e^{E_t(\bar{x})} = e^{E_t(x)}$$

Table 7 (Non-) Stationarity of Log Dividend–price Ratios.

		Autocorrelations					Unit root test	
		AC(1)	AC(2)	AC(3)	AC(6)	AC(12)	$t(ADF)$	$p(ADF)$
ln <i>D/P</i>	SMI	0.94	0.89	0.84	0.71	0.49	−2.60	>0.1
	S&P500	0.92	0.82	0.73	0.45	0.00	−2.89	>0.1
	DAX	0.92	0.84	0.78	0.61	0.27	−2.42	>0.1
	EUROSTOXX50	0.93	0.85	0.80	0.60	0.28	−2.53	>0.1

Notes: ln *D/P* denotes the logarithmic dividend–price ratio. SMI refers to the Swiss stock market, S&P500 to the US stock market, DAX to the German stock market and EUROSTOXX50 to the major stocks of the Euro area. Monthly data are used from January 2006 to December 2018.

ADF: Augmented Dickey–Fuller test, constant and trend, Lags = 0, BIC-criterion.

$p(ADF) > 0.1$ indicates that the null hypothesis of a unit root cannot be rejected on a 90% confidence level.

where averages are computed from n observations. Equation (8) can then be expressed as

$$\lim_{n \rightarrow \infty} E_t(1 + \bar{R}_g) \approx \frac{D_{t+1}}{P_t} + \lim_{n \rightarrow \infty} E_t \left(1 + \frac{\overline{\Delta D}}{D_g} \right) \quad (9)$$

where \bar{R}_g is the geometric average of discrete (arithmetic) returns, and $\overline{\Delta D}/D_g$ is the geometric average of relative (percentage) changes in dividends.¹⁵ In terms of the implied Gordon parameters the equation reads as

$$k_t = \frac{D_{t+1}}{P_t} + w_t \quad (10)$$

which corresponds to Campbell's characterization: although the setting is stochastic, a Gordon-like relationship is valid: the parameters can be interpreted as long-run conditional expectations, but in terms of *geometric* averages respectively logarithmic growth rates. This is a very simple way to incorporate parameter uncertainty and a volatile D/P -ratio into the Gordon formula.

4.2 Steady-state interpretation

The original Gordon formula is often interpreted as a conditional steady-state expression for the market value of equities: while the parameters are time-dependent, the D/P -ratio must be stationary in the sense that it exhibits no unconditional volatility:

$$\text{Var} \left(\ln \frac{D_{t+1}}{P_t} \right) = 0 \quad (11)$$

This is Campbell's interpretation of the "original" Gordon model and represents a limiting case of his model. This interpretation has an interesting implication:

In Campbell's model, a zero variance of the D/P -ratio¹⁶ implies that the stock returns and dividend growth have the same variance. This relies on an approximation in Campbell's derivation, namely that the variability of the D/P -ratio does not add substantially to the variability of returns compared to the volatility of dividend growth. In the steady-state context, however, it is not an approximation but an *exact* result since the variance of D/P is zero! This moreover implies that, in the steady-state, return and dividend growth *levels*

Table 8 Conditional Means, Variances and Correlations of Implied Gordon Parameters: Levels.

		Mean	Volatility	Correlation (k, w)
Growth w	SMI	8.14%	2.39%	
	S&P500	10.48%	1.29%	
	DAX	7.16%	1.01%	
	EUROSTOXX50	6.05%	1.52%	
Discount rate k	SMI	11.38%	2.10%	0.984
	S&P500	12.57%	1.15%	0.985
	DAX	10.52%	0.92%	0.842
	EUROSTOXX5Q	10.12%	1.64%	0.911

Notes: Dividend growth (w) and the discount rate (k) are extracted from three valuation ratios (price-earnings, price-dividend, price-book) using the Gordon model. SMI refers to the Swiss stock market, S&P500 to the US stock market, DAX to the German stock market and EUROSTOXX50 to the major stocks of the Euro area. Monthly data are used from January 2006 to December 2018.

are perfectly correlated. As shown in Table 8, this is not far away from what we observe empirically in our implied parameters, except for Germany, where the correlation coefficient is 0.84.

If the stock returns and dividend growth have the same variance, it follows that Equation (8) holds with arithmetic—not geometric—averages

$$\lim_{n \rightarrow \infty} E_t(\bar{R}_a) \approx \frac{D_{t+1}}{P_t} + E_t \left(\frac{\overline{\Delta D}}{D} a \right) \quad (12)$$

which Campbell calls the “*arithmetic* implementation” which corresponds to the traditional interpretation of the original Gordon model. The reason is that a geometric average of a variable equals approximately the arithmetic average minus one-half the variance, i.e.

$$\bar{X}_g \approx \bar{X}_a - \frac{1}{2} \text{Var}(\ln(1 + X)) \quad (13)$$

This substitution is made for both geometric averages in Equation (9), and since both variances are equal under the steady-state assumption (11), they cancel out and the arithmetic interpretation of formula (12) follows.

4.3 Implications for steady-state parameters and valuation

A direct implication is that the implied Gordon parameters in our preceding analysis (w_{imp} , k_{imp}) which are extracted from the observed ratios cannot be interpreted as steady-state proxies per se, but as their geometric counterparts. For extracting implied steady-state values, the stationarity or zero D/P -variance assumption (11) is needed which requires a transformation to arithmetic parameters. This can be calculated using the approximation in Equation (13), i.e. by *adding* half a variance to the implied parameters.

Taking the implied Gordon parameters of the S&P500 as of December 2018 (see Section 1) and

the volatilities from Table 8,¹⁷ we calculate the steady-state values for the US market as

$$w_{SS} = \underbrace{0.1240}_{w_{imp}} + \frac{1}{2} 0.0129^2 = 0.1241$$

$$k_{SS} = \underbrace{0.1460}_{k_{imp}} + \frac{1}{2} 0.0115^2 = 0.1461$$

and reveals that the numerical effects are negligible, at least with our empirical estimates. It also reflects the observation that the volatilities of the implied k and w are roughly the same for the analyzed markets. This contrasts Campbell’s claim that “returns are much more volatile” (p. 11) compared to growth rates, but confirms our earlier finding that the volatility of growth rates and their change are often underestimated.

While the geometric versus arithmetic interpretation matters for the individual parameters *in principle* (but is not empirically relevant in our data), it has no consequences for the *valuation* effects in the steady-state because only the difference $k - w$ enters the Gordon formula in the denominator which is unaffected by the variances of k and w : an increase in the dividend variance leads to an identical increase of the return variance. This is a key property of Campbell’s stochastic version of the Gordon model, and might either be regarded as a major limitation or as a major strength of the model: what, assuming rational market valuation, should variations of steady-state discount rates reflect other than variations of steady-state dividend growth? More advanced models and a more elaborated steady-state characterization than (11) should eventually be able to disentangle the return variance from the dividend growth variance in the steady-state, but the present framework does not allow this.¹⁸

Another question relates to the valuation *bias* if Campbell’s geometric interpretation of the Gordon formula is used in empirical work for

inferring steady-state asset values instead the arithmetic interpretation. A high return volatility increases k_{SS} relative to the implied parameter and lowers equity values, i.e. steady-state values are overestimated by geometric parameters. The reverse bias results for dividend growth: a high variability increases w_{SS} relative to the implied parameter, but increases asset values. Thus, steady-state asset values are underestimated if geometric parameters are inadequately used. However, given the small values and, in particular, the small differences between the return and growth volatilities as shown in Table 8, the bias is very small in general. Therefore, the

implied Gordon parameters can be regarded as sufficiently good empirical proxies for analyzing steady-state valuation effects.

4.4 Persistence

Finally, Table 9 displays the time-series properties of the implied Gordon parameters (in levels): They are highly persistent, and the null hypothesis of a unit root cannot be rejected in almost all series. Highly persistent parameters should definitely be expected for conditional steady-state magnitudes. It strongly supports our claim that

Table 9 Time-series Properties of Implied Gordon Parameters: Levels.

		Autocorrelations					Unit root test	
		AC(1)	AC(2)	AC(3)	AC(6)	AC(12)	$t(ADF)$	$p(ADF)$
Reinvestment b	SMI	0.96	0.93	0.90	0.81	0.64	-3.09	>0.1
	S&P500	0.98	0.95	0.92	0.80	0.48	-1.32	>0.1
	DAX	0.97	0.93	0.88	0.70	0.27	-1.82	>0.1
	EUROSTOXXSO	0.96	0.92	0.88	0.72	0.46	-2.21	>0.1
Profitability r	SMI	0.92	0.86	0.80	0.67	0.27	-3.12	>0.1
	S&P500	0.96	0.92	0.87	0.68	0.26	-0.76	>0.1
	DAX	0.96	0.91	0.85	0.59	-0.08	-2.03	>0.1
	EUROSTOXXSO	0.98	0.96	0.93	0.84	0.64	-1.46	>0.1
Growth w	SMI	0.95	0.91	0.87	0.77	0.51	-2.98	>0.1
	S&P500	0.96	0.92	0.87	0.67	0.19	-1.03	>0.1
	DAX	0.96	0.92	0.86	0.62	0.04	-1.95	>0.1
	EUROSTOXXSO	0.98	0.95	0.92	0.82	0.60	-1.71	>0.1
Discount rate k	SMI	0.93	0.88	0.84	0.74	0.52	-3.37	0.06
	S&P500	0.95	0.90	0.85	0.65	0.19	-1.12	>0.1
	DAX	0.93	0.86	0.79	0.49	-0.04	-2.56	>0.1
	EUROSTOXX5Q	0.97	0.94	0.92	0.81	0.62	-1.79	>0.1

Notes: Autocorrelations (AC) at lags 1, 2, 3, 6, and 12 of levels of reinvestment rate (b), profitability (r), growth (w) and discount rate (k) extracted from three valuation ratios (price-earnings, price-dividend, price-book) using the Gordon model. SMI refers to the Swiss stock market, S&P500 to the US stock market, DAX to the German stock market and EUROSTOXX50 to the major stocks of the Euro area. Monthly data are used from January 2006 to December 2018. ADF: Augmented Dickey-Fuller test, constant and trend, Lags = 0, BIC-criterion. $p(ADF) > 0.1$ indicates that the null hypothesis of a unit root cannot be rejected on a 90% confidence.

implied Gordon parameters, as extracted by our approach, provide insight into the steady-state properties of market fundamentals.

5 Summary and Discussion

Market fundamentals (discount rates, growth rates, profitability, etc.) extracted from widely used valuation ratios using the Gordon model provide insight into the long-run expectations implicit in stock market prices. In this paper, several key statistical properties of the implied market parameters are analyzed and put into relation to well-known results from the asset pricing literature. Our key finding is that the statistical behavior differs in several important ways. The implied Gordon parameters predict a substantially larger volatility of growth rates than most predictive models, and the growth rate is positively and occasionally extremely highly correlated with the discount rate.

These properties have important implications for the valuation of equities and are in stark contrast to similar findings in the empirical literature. For example, the variability of the expected growth rate invalidates the interpretation of variations in D/P -ratios as a direct proxy of revisions in long-run expected returns. And the *positive* association between changes in growth and discount rates suggests a completely different interpretation of the cyclicity of risk premiums compared to, for example, conditional asset pricing models estimated with typical state variables (“business conditions”). This also leads to a different interpretation of expected and unexpected returns over valuation cycles: e.g., if accelerated growth expectations are neglected in the roaring 1990s, expected returns and risk premiums must be larger to be consistent with observed dividend–price ratios, hence a smaller fraction of observed large returns is unexpected.

Of course, one might object that the (long)-time horizon to which the implied Gordon parameters refer are distinct to the (short) horizon of many asset pricing models. Therefore, we hypothesize that our risk premiums are related to long-run growth risk. However, it is interesting to observe that the dynamic properties of the implied Gordon estimates are also in contrast to the results found in the “long-run risk” (LRR) literature. There, we observe only slightly positive correlations between discount rate and cash flow (growth) “news” at best, but mostly zero or even negative correlations. High correlations between discount rates and growth rates as found in this paper exert a damping influence on the stock return volatilities. Hence, stock returns may still be very volatile relative to the underlying economic fundamentals and their expectations, but the correlation pattern suggested by the implied Gordon parameters suggests a stabilizing effect for the relevant—infinately long—time horizon.

These observations suggest that information extracted from valuation ratios, using simple valuation models, differs from the estimates relying on econometric models using historical returns. We argue, in the spirit of Campbell (2008), that implied Gordon parameters can be interpreted as empirical *proxies* for conditional steady-state market fundamentals. Campbell’s model which assumes a Random Walk for the dividend-price ratio also provides a justification for using the Gordon formula—which in its original version assumes constant parameters—for extracting time-varying parameters. The steady-state can then be defined as limiting case where the D/P -ratio is stationary in the sense that it exhibits no unconditional volatility. Our interpretation of the implied Gordon-parameters as good empirical *proxies* of steady-state fundamentals is reinforced by the highly persistent behavior of the parameters which be expected for conditional steady-state variables.

Notice that all estimations in this paper are based on the simple Gordon formula. This may be an oversimplified model even for a steady-state interpretation. It would be intriguing to learn the steady-state implications of richer models.

6 Implications

The empirical insights of this paper have many interesting implications. The most important is of course how the implied parameters, which represent conditional expectations, are related to actual future returns and growth rates. Campbell and Thomson (2008) provide encouraging evidence that prior's from fundamental ratios significantly improves predictability of returns: "Even better results can be obtained by imposing the restrictions of steady-state valuation models, thereby removing the need to estimate the average from a short sample of volatile stock returns." Lettau and Van Nieuwerburgh (2007) find that inconsistent results between in-sample and out-of-sample predictability tests can be explained by parameter instability and claim that "these seemingly incompatible results can be reconciled if the assumption of a fixed steady-state mean of the economy is relaxed." An even more interesting question is how well steady-state risk factors—i.e. growth risk and its components—perform in cross-sectional asset pricing tests compared to LRR-related news factors. Therefore, steady-state analysis of market fundamentals offers an interesting and important field for future empirical research.

The findings of this paper also offer new insights for investors who base their decisions on fundamental valuation factors and assume a (very) long valuation horizon. They should compute implied market fundamentals jointly from several valuation ratios using a valuation model (not necessarily Gordon), which contradicts widely used, univariate rules-of-thumb such as "an increasing

P/E-ratio indicates improved growth expectations". In addition, this paper shows that implied parameters are highly persistent which means that their changes are not so quickly reversed. This does not mean that actual market fundamentals are slowly changing, but that their long-run expectations as reflected in market values do. If an investor has better information to change her long-run views, she could benefit from contrasting her views to those reflected in the implied parameters. Moreover, investors should be aware that (very) long-run return expectations are most likely to exhibit a cyclical—not countercyclical—pattern, which differs from a tactical (monthly or quarterly) view of markets. This could have a substantial impact on the asset allocation decisions of investors with a long-term investment horizon. This application is left for future research.

Appendix: Data

Valuation multiples:

Valuation multiples are downloaded from Bloomberg. *P/E*-ratios (BEST_PE_RATIO) rely on estimated earnings of the four subsequent quarters (Bloomberg estimates). *P/D*-ratios are the reciprocal values of the dividend yields (BEST_DIV_YLD) which rely on estimated dividends of the subsequent 12 months (Bloomberg estimates). *P/B*-ratios (BEST_PX_BPS_RATIO) relate market prices to estimated book values (Bloomberg estimates). End-of-month values are used throughout the analysis.

Risk-free interest rates:

Swiss-franc denominated risk-free interest rates are spot rates for a time horizon of 20 years calculated from government bonds. End-of-month observations are used (source: Swiss National Bank). A long-run maturity is selected since the discounting horizon of the Gordon model is infinite. For Germany and the

Eurostoxx50 countries, Euro-denominated risk-free interest rates are spot rates for a time horizon of 20 years extracted from listed Federal securities. End-of-month observations are used (source: Deutsche Bundesbank).

USD-denominated risk-free interest rates are yields on government bonds with a maturity of 20 years. Only monthly averages are available (source: FRED database, Federal Reserve Bank of St. Louis). Thus, risk-free interest rates—and thus risk premiums—are not directly comparable to the spot rates used for Switzerland, Germany and the Eurostoxx50 countries.

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Endnotes

- ¹ Notice that in the context of the Gordon formula, this ratio relates the *end-of-period* dividend (which is assumed to be known) to the current stock price; the expression is usually referred to as “dividend yield”. In the empirical specification of the variable, the variable is proxied by the Bloomberg “best estimate” dividend yield. However, in the wording of this paper, the term “dividend–price ratio” is used for consistency reasons with the other ratios.
- ² All the subsequent results are related to first differences unless stated otherwise.
- ³ For better readability, all numbers are multiplied by 10,000 in the variance expression.
- ⁴ The figures moreover reveal very high fluctuations in the dividend payout. As discussed in Zimmermann (2018), the payout policy in Switzerland was rather special over the analyzed time period, due to special fiscal circumstances. For the other countries, the dividend payout ratios are rather stable.
- ⁵ Notice that the implied Gordon parameters refer to an infinite horizon.
- ⁶ The term “long-run risk models” is not an established wording, but is mostly related to the research following Bansal and Yaron (2004). Here, the term is used for all papers following Campbell and Shiller (1988), Campbell (1991), and subsequent paper, including statistical models as well as equilibrium models.
- ⁷ The term “cash flow” news (or CF risk) is used in models for explaining the variability of fundamental stock valuation ratios, while “growth” news (or growth risk) is used in macroeconomic models about the variability of consumption growth or consumption-wealth ratios (Campbell, 1996; Bansal and Yaron, 2004, etc.).
- ⁸ Still, the period of the Campbell and Vuolteenaho (2004) study is from 1928 to 2001 and does not overlap with our sample period. If estimated with more recent data, Séchaud and Zimmermann (2021) find that the correlation of DR- and CF-news for the US stock market is fairly unstable across subperiods, but not substantially larger than those reported in the text. Also, the results are not different if real data is used. However, the correlations are substantially larger (up to 0.79) between DR- and CF-news in the US REIT-market.
- ⁹ In the Bansal–Yaron models, growth risk is related to consumption growth, not dividend growth. We do not make this distinction here and simply refer to “cash flows”.
- ¹⁰ This condition can be most easily be seen in Bansal *et al.* (2012), from their λ_e -term in Equations (10) and (11).
- ¹¹ Havranek *et al.* (2015) provide a particularly useful meta-analysis on this subject. The authors evaluate 2,735 estimates of the elasticity of intertemporal substitution in consumption in 169 published studies that cover 104 countries during different time periods. While the average estimate is well below one, they find that “‘households in rich countries and countries with high stock market participation substitute a larger fraction of consumption intertemporally in response rate changes.”
- ¹² Notice that in finite samples, the persistence of a process is underestimated by autocorrelation coefficients.
- ¹³ A third assumption is trivial in our setting, namely that the end-of-period dividend is known one period in advance. See Footnote (1). Notice that the Random Walk assumption for the *DIP*-ratio is not uncritical. Some

authors see a non-stationary dividend as a proof of bubbles (e.g. Craine, 1993), while others claim that this conclusion is invalid (e.g. Bidian, 2014).

- ¹⁴ The restatement uses (a) the relation between the log of expectations and the expectation of logs, which is given by half of the variance of the log; and (b) the linear approximation $1 + y \approx \exp(y)$. Notice that Campbell (2008) does not distinguish between the conditional one-period expectation and the expectation of geometric averages; he interprets the expectations in Equation (7) directly as “geometric averages”, which is not exactly correct.
- ¹⁵ To clarify the notation: $r = \ln(1 + R)$ and $\Delta d = \ln(1 + \Delta D/D)$. Notice that the bar and the subscript g in $\bar{\Delta D}/\bar{D}_g$ are both related to the entire ratio.
- ¹⁶ Remember that there are two sources of uncertainty in the model: log D/P growth and dividend growth. The variance of the returns (discount rate) is derived *endogenously* from the model.
- ¹⁷ Notice that these are conditional means and variances, since the historical values of implied parameters are conditional expectations, i.e. reflect the current state of information about the future.
- ¹⁸ A dynamic choice model which characterizes a “risky steady-state” can be found in Coeurdacier *et al.* (2011); it predicts a positive impact of income (dividend) uncertainty on steady-state wealth in the cross-section of households or countries.

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